

NATIONAL PH.D. PROGRAM IN AUTONOMOUS SYSTEMS

A nonlinear dynamical approach to the symptoms graph

Ph.D. candidate

Iacopo CAPOROSSI

Cycle XL

Tutors

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1. Description of the research program

Recently a group of psychologists proposed the use of graphs to represent mental disorders (called symptoms graph), in which the graph's nodes represent the symptoms of the mental illness and the edges are the connections between them. One of the main results they obtained is that a necessary condition for having a mental disorder is the strong connectivity of the symptoms graph.

In my master thesis I introduced the evolution over time in the symptoms graph assuming some simplifications: the adjacency matrix is fixed and the external triggers that activates one or more symptoms appears only once (at beginning). I obtained a linear dynamical system in which the variables are the symptoms of the mental disorder which can be either active, setting the variable 1, or inactive, setting the variable 0. Performing numerical simulations (using a Matlab code) and using synchronization's theory, the conclusion is that a peculiar case for which one can talk about recovery from a mental disorder is reaching a consensus under a certain threshold.

In my thesis the symptoms graph has been constructed analyzing transcribed therapy sessions, in my PHD I propose to use NLP's techniques to let the symptoms graph be constructed in an automated way. In order to built the required data collection to train the artificial intelligence, agreements with Scuola di Psicoterapia Integrativa Interdisciplinare (SPII) of Florence were made in order to obtain complete and transcribed therapy paths to be analyzed.

The second task that I propose to investigate in my PHD is the relationship between the psychological concept of hysteresis and its mathematical counterpart. A psychological definition of hysteresis can be the tendency of the individuals to keep performing some behaviors, even if some parameters are changed. Borsboom and Cramer found that if the graph reacting to the symptoms' activation due to an external trigger becomes strongly connected, the symptoms keep staying active even if the external trigger (the modification on the nearby patient) disappears. Whereas, in dynamical systems' theory, the hysteresis can be defined as a sort of delay in responding to the perturbations in relation with the previous state.

The study will be divided following these steps, at the first the discrete time linear system developed in my thesis will be expanded in continuous time, supposing that the activation function of every symptom depends in a linear way (to maintain the adjacency matrix structure) to the others. Then we perturb the system adding a nonlinear term in one symptom with the claim of finding necessary conditions on the adjacency matrix and on the nonlinear term to have an hysterical regime in the perturbed system. As a final result, the generalization of it, adding the nonlinear term in a general number of symptoms will be study.

2. Schedule of the research activities

First academic year planned

| | Description | Period | Activity abroad |
|-------------------------------|---|-------------|-----------------|
| Study the relevant literature | Analyze the the state of art of the relevant literature in matter of psychological complex systems and machine learning techniques. | 1-12 months | NO |
| Application to my model | Expand the existing linear model introducing nonlinearity to better describe the evolution over time of a mental disorder from a theoretical point of view. | 1-12 months | NO |

Second academic year planned

| | Description | Period | Activity abroad |
|---|--|------------|-------------------------|
| Data collection and collaboration with Prometeo | Collaboration with the company Prometeo (up to 6 months) Collections of transcribed therapy paths to let the construction of the symptoms graph be automatized. | 1-12 month | NO |
| Validation of the model | Collaboration with psychologists to validate the proposed model | 9 month | NO |
| Period abroad | Studying similar model based on different hypothesis | 3 months | YES (to be acknowledge) |

Third academic year planned

| | Description | Period | Activity abroad |
|-------------------------|--|-------------|-------------------------|
| Analysis of the results | Analysis of the results obtained with the aim of developing a more adherent with reality model | 3 months | YES (to be acknowledge) |
| Writing the PHD thesis | Writing the PHD thesis | 1-12 months | NO |

3. Training and research activities plan

First academic year planned

| | | Description | Period | Final Exam | ECTS |
|----|--|--|----------------|---------------|------|
| A. | Ph.D. courses | Complex Network Theory: theory, methods and applications | March | Yes | 2 |
| | | Linear Algebra for control applications | Feb-Mar | Yes | 2 |
| | | Introduction to Autonomous Systems | June | Yes | 1 |
| В. | Master's degree courses | Programming for data science | Nov- Jen | Yes | 6 |
| C. | Soft skill courses | Partecipation to one soft skill courses according to availability | 1-12 months | Yes | 2 |
| D. | Participation to seminars | Participation to at least four seminars according to availability. | 1-12 months | No | 7,5 |
| E. | Participation to international congresses or workshops | Participation to at least one international congresses or workshops according to availability. | 1-12 months | No | 2 |
| F. | Presentation of research products at international congresses or workshops | Presentation of the results obtained to at least one international congresses or workshops. | 1-12 months | No | 2 |
| | | TOTAL OF ECTS FOR TRAINING ACTIVITIE | S | | 24.5 |
| G. | Individual research activity | Research activities in the field of networked systems and NLP's techniques. | 1-12 months | No | 15,5 |
| Н. | Supervision of students | Supervision of Students under the guidance of the tutor. | 1-12 months | No | 5 |
| I. | Integrative teaching activities | Integrative didactive activities to be carried out under the supervision of the tutor. | 1-12 months | No | 5 |
| J. | Preparation of manuscripts for conferences or journals | Verbalization of the results obtained, in the form of a paper for a conference or a journal. | 1-12 months | No | 10 |
| | | TOTAL OF ECTS FOR RESEARCH ACTIVITIES TOTAL OF ECTS | | | 35,5 |
| | | | | | 60 |

Second academic year planned

| | | Description | Period | Final Exam | ECTS |
|----|--|--|----------------|---------------|------|
| A. | Ph.D. courses | Participation to at least four PhD courses according to availability. | 1-12 months | Yes | 7 |
| В. | Master's degree courses | | | | |
| C. | Soft skill courses | Participation to one soft skill course according to availability | 1-12 months | No | 2 |
| D. | Participation to seminars | Participation to at least two seminars according to availability. | 1-12 months | No | 3 |
| E. | Participation to international congresses or workshops | Participation to at least one international congresses or workshops according to availability. | 1-12 months | No | 2 |
| F. | Presentation of research products at international congresses or workshops | Presentation of the results obtained to at least one international congresses or workshops. | 1-12 months | No | 2 |
| | | TOTAL OF ECTS FOR TRAINING ACTIVITIE | S | | 16 |
| G. | Individual research activity | Research activities in the field of networked systems and NLP's techniques. | 1-12 months | No | 17 |
| Н. | Supervision of students | Supervision of Students under the guidance of the tutor. | 1-12 months | No | 7 |
| I. | Integrative teaching activities | Integrative didactive activities to be carried out under the supervision of the tutor. | 1-12 months | No | 10 |
| J. | Preparation of manuscripts for conferences or journals | Verbalization of the results obtained, in the form of a paper for a conference or a journal. | 1-12 months | No | 10 |
| | | TOTAL OF ECTS FOR RESEARCH ACTIVITIES | | | 44 |
| | TOTAL OF ECTS | | | | 60 |

Third academic year planned

| | | Description | Period | Final Exam | ECTS |
|----|--|--|----------------|---------------|------|
| A. | Ph.D. courses | | | | |
| В. | Master's degree courses | | | | |
| C. | Soft skill courses | | | | |
| D. | Participation to seminars | Participation to at least two international congresses or workshops according to availability. | 1-12 months | No | 4 |
| Е. | Participation to international congresses or workshops | Participation to at least two international congresses or workshops according to availability. | 1-12 months | No | 4 |
| | | TOTAL OF ECTS FOR TRAINING ACTIVITIE | S | | 8 |
| G. | Individual research activity | Research activities in the field of networked systems and NLP's techniques. | 1-12 months | No | 20 |
| Н. | Supervision of students | Supervision of Students under the guidance of the tutor. | 1-12 months | No | 12 |
| I. | Integrative teaching activities | Integrative didactive activities to be carried out under the supervision of the tutor. | 1-12 months | No | 10 |
| J. | Preparation of manuscripts for conferences or journals | Verbalization of the results obtained, in the form of a paper for a conference or a journal. | 1-12 months | No | 10 |
| | | TOTAL OF ECTS FOR RESEARCH ACTIVITIES | | | 52 |
| | | TOTAL OF ECTS | | | 60 |

4. List of the publications written by the candidate in the triennium

Master Thesis of M.Sc. Program in Applied Mathematics

Caporossi I., A dynamical approach to the symptoms graph, University of Siena (July 18-th 2024)

International Conference Proceedings

Caporossi I., Vitanza E., Mocenni C., A nonlinear dynamical model of the symptoms graph, Conference of complex systems CCS2024, Exeter, September 1-st - 7-th 2024 (postere presentation)

